Centre Number			Candidate Number		
Surname					
Other Names					
Candidate Signature					



General Certificate of Education
Advanced Subsidiary Examination
June 2015

Mathematics

MFP1

Unit Further Pure 1

Friday 5 June 2015 9.00 am to 10.30 am

For this paper you must have:

• the blue AQA booklet of formulae and statistical tables. You may use a graphics calculator.

Time allowed

• 1 hour 30 minutes

Instructions

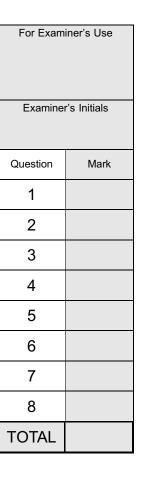
- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer all questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.





Answer all questions.

Answer each question in the space provided for that question.

- **1** The quadratic equation $2x^2 + 6x + 7 = 0$ has roots α and β .
 - (a) Write down the value of $\alpha + \beta$ and the value of $\alpha\beta$.

[2 marks]

(b) Find a quadratic equation, with integer coefficients, which has roots α^2-1 and β^2-1 .

[5 marks]

(c) Hence find the values of α^2 and β^2 .

[2 marks]

QUESTION PART REFERENCE	Answer space for question 1



QUESTION PART REFERENCE	Answer space for question 1



2 (a)	Explain why	$\int_{0}^{4} \frac{x-4}{x^{1.5}} dx$ is an improper integral
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[1 mark]

(b) Either find the value of the integral $\int_0^4 \frac{x-4}{x^{1.5}} dx$ or explain why it does not have a finite value.

[4 marks]

QUESTION PART REFERENCE	Answer space for question 2



QUESTION PART REFERENCE	Answer space for question 2



- 3 (a) Show that $(2+i)^3$ can be expressed in the form 2+bi, where b is an integer. [3 marks]
 - (b) It is given that 2 + i is a root of the equation

$$z^3 + pz + q = 0$$

where p and q are real numbers.

(i) Show that p = -11 and find the value of q.

[4 marks]

(ii) Given that $2-{\rm i}$ is also a root of $z^3+pz+q=0$, find a quadratic factor of z^3+pz+q with real coefficients.

[2 marks]

(iii) Find the real root of the equation $z^3 + pz + q = 0$.

[2 marks]

QUESTION PART REFERENCE	Answer space for question 3



QUESTION PART REFERENCE	Answer space for question 3



4 (a) Find the general solution, in degrees, of the equation

$$2\sin(3x+45^\circ)=1$$

[5 marks]

(b) Use your general solution to find the solution of $2\sin(3x+45^\circ)=1$ that is closest to 200° .

[1 mark]

QUESTION PART REFERENCE	Answer space for question 4



QUESTION PART REFERENCE	Answer space for question 4



5 (a) The matrix **A** is defined by $\mathbf{A} = \begin{bmatrix} -2 & c \\ d & 3 \end{bmatrix}$.

Given that the image of the point (5, 2) under the transformation represented by **A** is (-2, 1), find the value of c and the value of d.

[4 marks]

- **(b)** The matrix ${\bf B}$ is defined by ${\bf B}=\begin{bmatrix} \sqrt{2} & \sqrt{2} \\ -\sqrt{2} & \sqrt{2} \end{bmatrix}$.
 - (i) Show that ${\bf B}^4=k{\bf I}$, where k is an integer and ${\bf I}$ is the 2×2 identity matrix.

[2 marks]

(ii) Describe the transformation represented by the matrix ${\bf B}$ as a combination of two geometrical transformations.

[5 marks]

(iii) Find the matrix ${\bf B}^{17}$.

[2 marks]

QUESTION PART REFERENCE	Answer space for question 5



QUESTION PART REFERENCE	Answer space for question 5



QUESTION PART REFERENCE	Answer space for question 5



QUESTION PART REFERENCE	Answer space for question 5



6 A curve C_1 has equation

of C_2 .

$$\frac{x^2}{9} - \frac{y^2}{16} = 1$$

- (a) Sketch the curve C_1 , stating the values of its intercepts with the coordinate axes. [2 marks]
- (b) The curve C_1 is translated by the vector $\begin{bmatrix} k \\ 0 \end{bmatrix}$, where k < 0, to give a curve C_2 . Given that C_2 passes through the origin $(0, \, 0)$, find the equations of the asymptotes

[3 marks]

QUESTION PART REFERENCE	Answer space for question 6



QUESTION PART REFERENCE	Answer space for question 6



- 7 (a) The equation $2x^3 + 5x^2 + 3x 132000 = 0$ has exactly one real root α .
 - (i) Show that α lies in the interval $39 < \alpha < 40$.

[2 marks]

(ii) Taking $x_1=40$ as a first approximation to α , use the Newton–Raphson method to find a second approximation, x_2 , to α . Give your answer to two decimal places.

[3 marks]

(b) Use the formulae for $\sum_{r=1}^{n} r^2$ and $\sum_{r=1}^{n} r$ to show that

$$\sum_{r=1}^{n} 2r(3r+2) = n(n+p)(2n+q)$$

where p and q are integers.

[5 marks]

(c) (i) Express $\log_8 4^r$ in the form λr , where λ is a rational number.

[1 mark]

(ii) By first finding a suitable cubic inequality for k, find the greatest value of k for which $\sum_{r=k+1}^{60} (3r+2)\log_8 4^r \text{ is greater than } 106\,060\,.$

[4 marks]

REFERENCE	



QUESTION PART REFERENCE	Answer space for question 7



QUESTION PART REFERENCE	Answer space for question 7



QUESTION PART REFERENCE	Answer space for question 7



8 A curve C has equation

$$y = \frac{x(x-3)}{x^2+3}$$

(a) State the equation of the asymptote of C.

[1 mark]

(b) The line y = k intersects the curve C. Show that $4k^2 - 4k - 3 \le 0$.

[5 marks]

(c) Hence find the coordinates of the stationary points of the curve C.

(No credit will be given for solutions based on differentiation.)

[5 marks]

QUESTION PART REFERENCE	Answer space for question 8



QUESTION PART REFERENCE	Answer space for question 8



QUESTION PART REFERENCE	Answer space for question 8



QUESTION PART REFERENCE	Answer space for question 8
	END OF QUESTIONS



